

# Vacuum Acceleration in the Field of a Tightly Focused Laser

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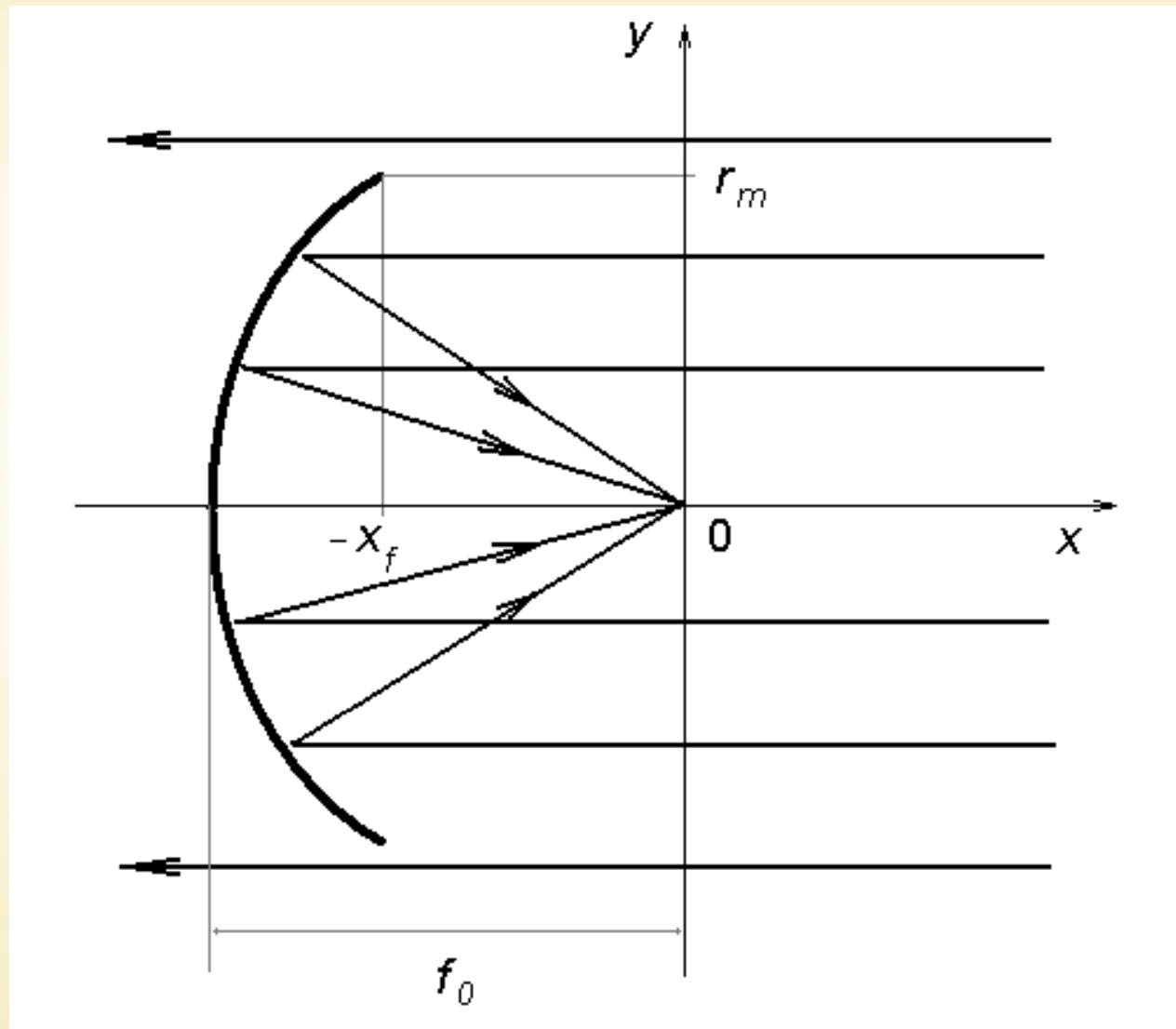
# Introduction

- We consider the problem of direct acceleration of electrons by the laser in vacuum
- Tight focusing is used to acquire high laser intensities
- In this regime we cannot use the paraxial approximation

# Methodology

- Correct field representation being a solution to the Maxwell equations is required
- Numerical solution for both fields and equations of motion needs to be employed
- Test particle approach is used for general understanding of the acceleration process
- Particle-in-cell (PIC) simulation is used for more realistic laser-plasma interaction

# Focusing of the laser by a parabolic mirror



$$f_{\#} = \frac{2r_m}{f_0}$$

Typical laser parameters:

$P \sim 100$  TW, mirror  $f_{\#} \sim 1$ , pulse length  $\sim 30$  fs, max. intensity in focus  $\sim 10^{22}$  W/cm<sup>2</sup>

# Stratton-Chu integrals\*

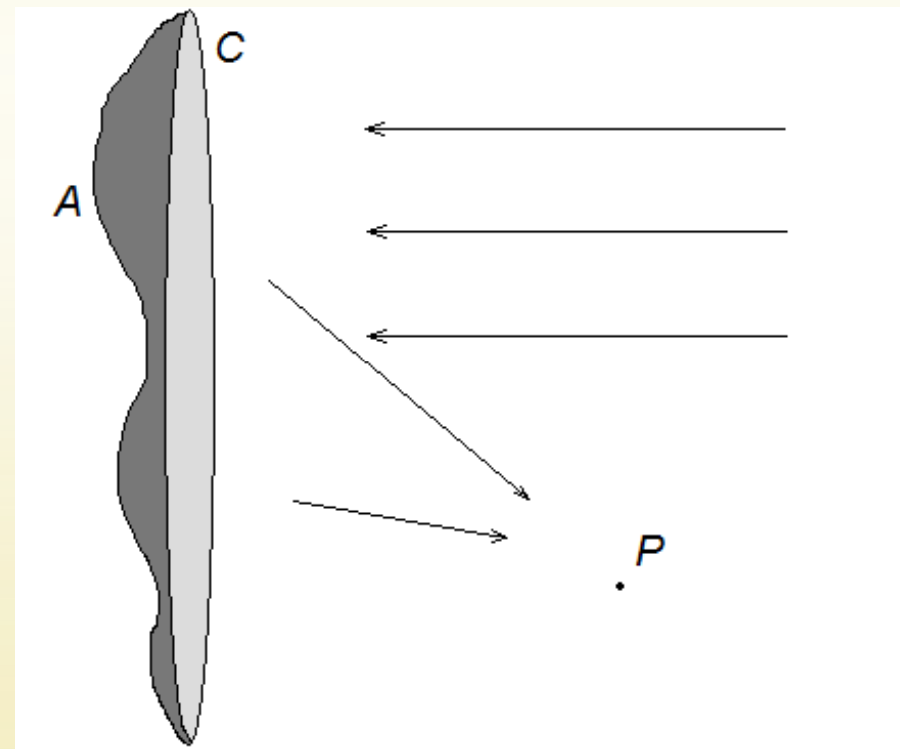
$$\vec{E}(P) = \frac{1}{4\pi} \iint_A \left[ jk (\vec{n} \times \vec{H}) G + (\vec{n} \times \vec{E}) \times \nabla G + (\vec{n} \cdot \vec{E}) \nabla G \right] dA,$$

$$\vec{H}(P) = \frac{1}{4\pi} \iint_A \left[ jk (\vec{E} \times \vec{n}) G + (\vec{n} \times \vec{H}) \times \nabla G + (\vec{n} \cdot \vec{H}) \nabla G \right] dA$$

$$G = \frac{\exp(jk|\vec{r}_A - \vec{r}_P|)}{|\vec{r}_A - \vec{r}_P|},$$

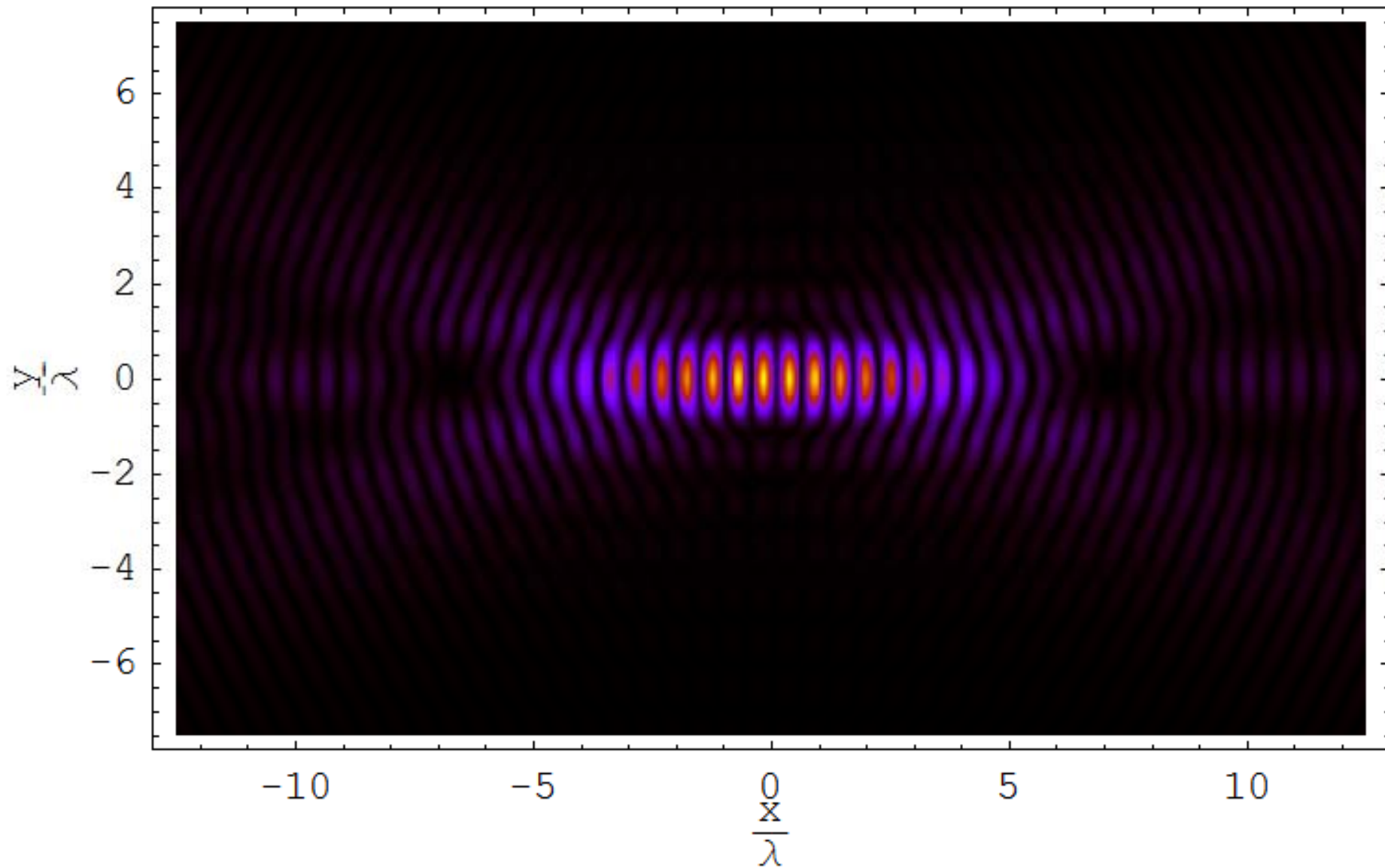
$$k = \frac{\omega_\lambda}{c},$$

$\vec{n}$  – inner normal to the surface



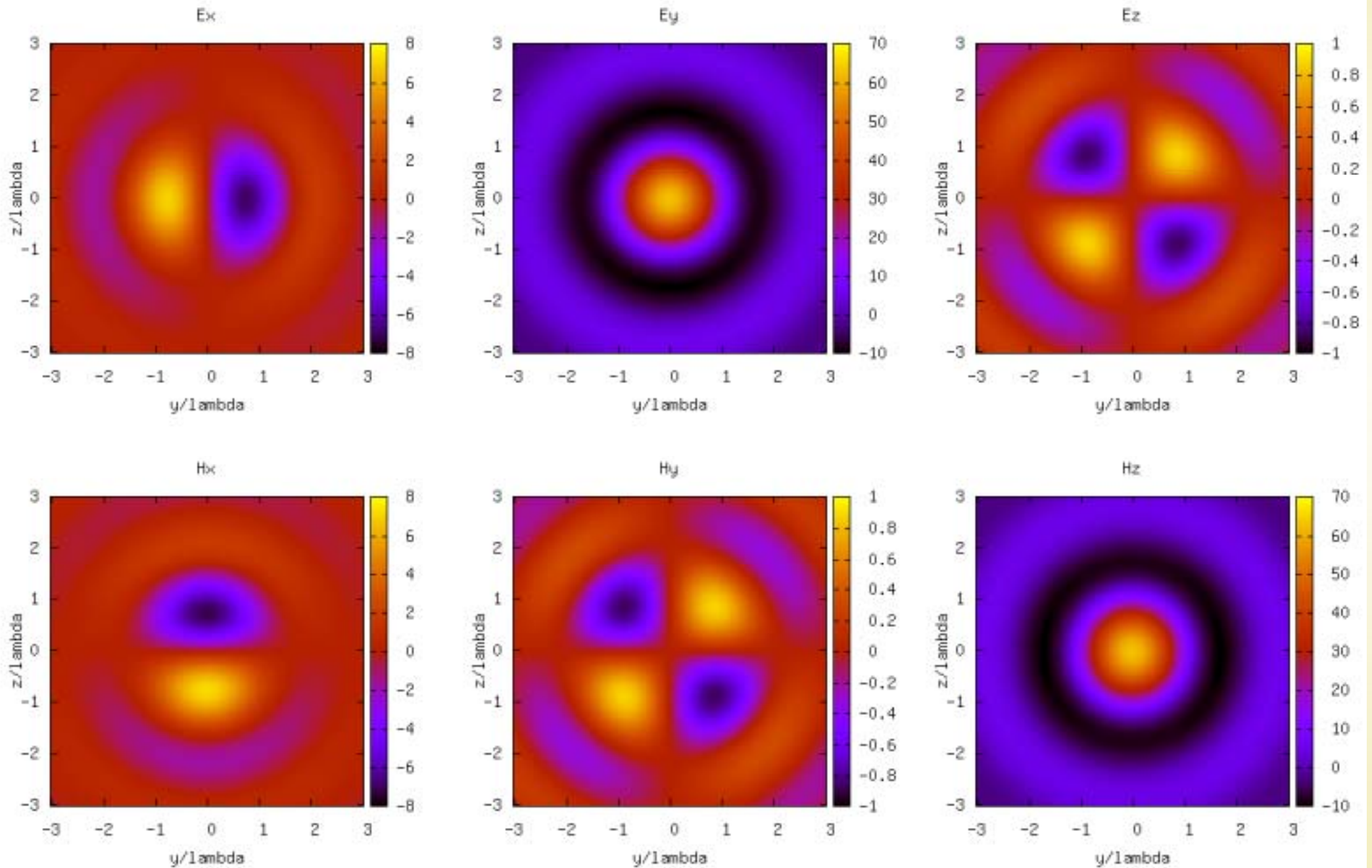
\*J.Stratton, L.Chu. "Diffraction Theory of Electromagnetic Waves", Phys. Rev. 56 ,99 (1939)

# Focused pulse structure



Poynting vector for  $f_{\#}=1$

# Electromagnetic field in the focus

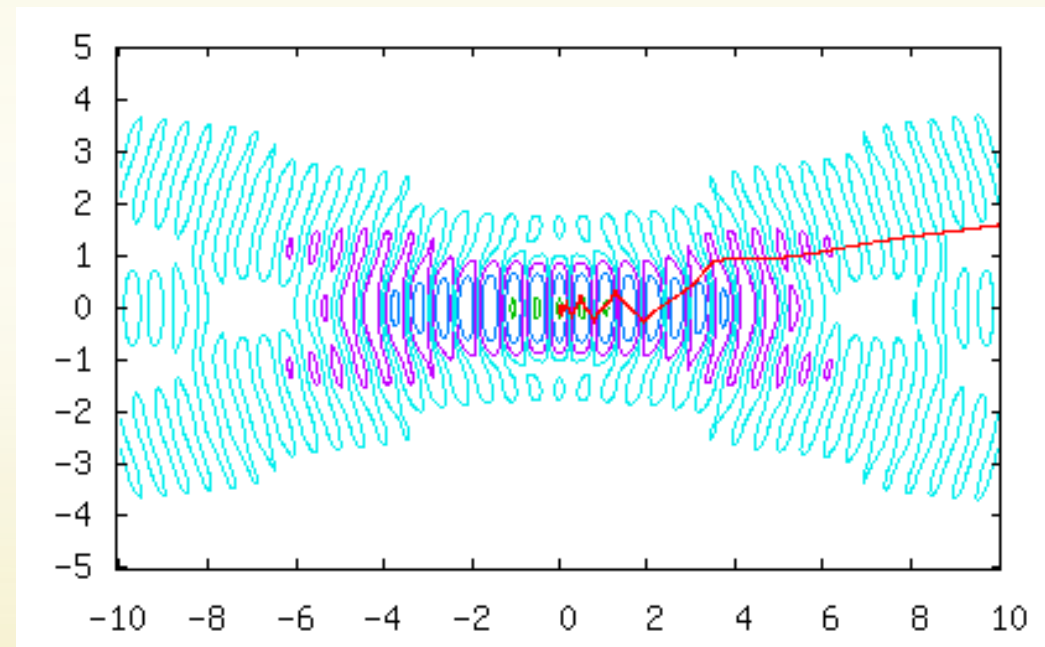


# Test particle acceleration\*

Motion of a single particle in the known electromagnetic field

$$\frac{d(\gamma m \vec{v})}{dt} = q(\vec{E} + \vec{v} \times \vec{B})$$

Trajectory of a particle started from the best focus:

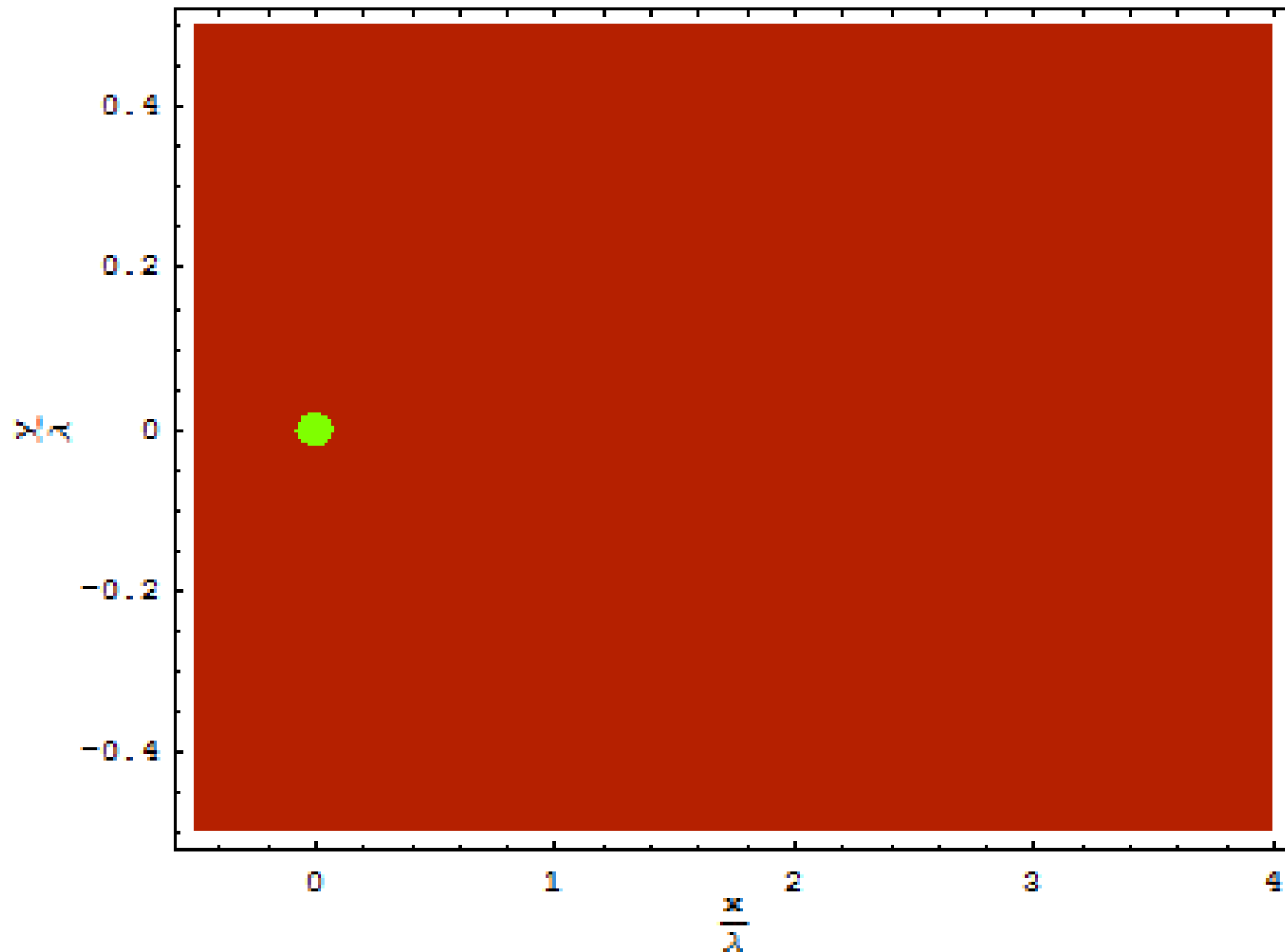


Particles are able to acquire non-zero energy in the acceleration process because of high field nonlinearities causing asymmetry between the initial and final states of the particle

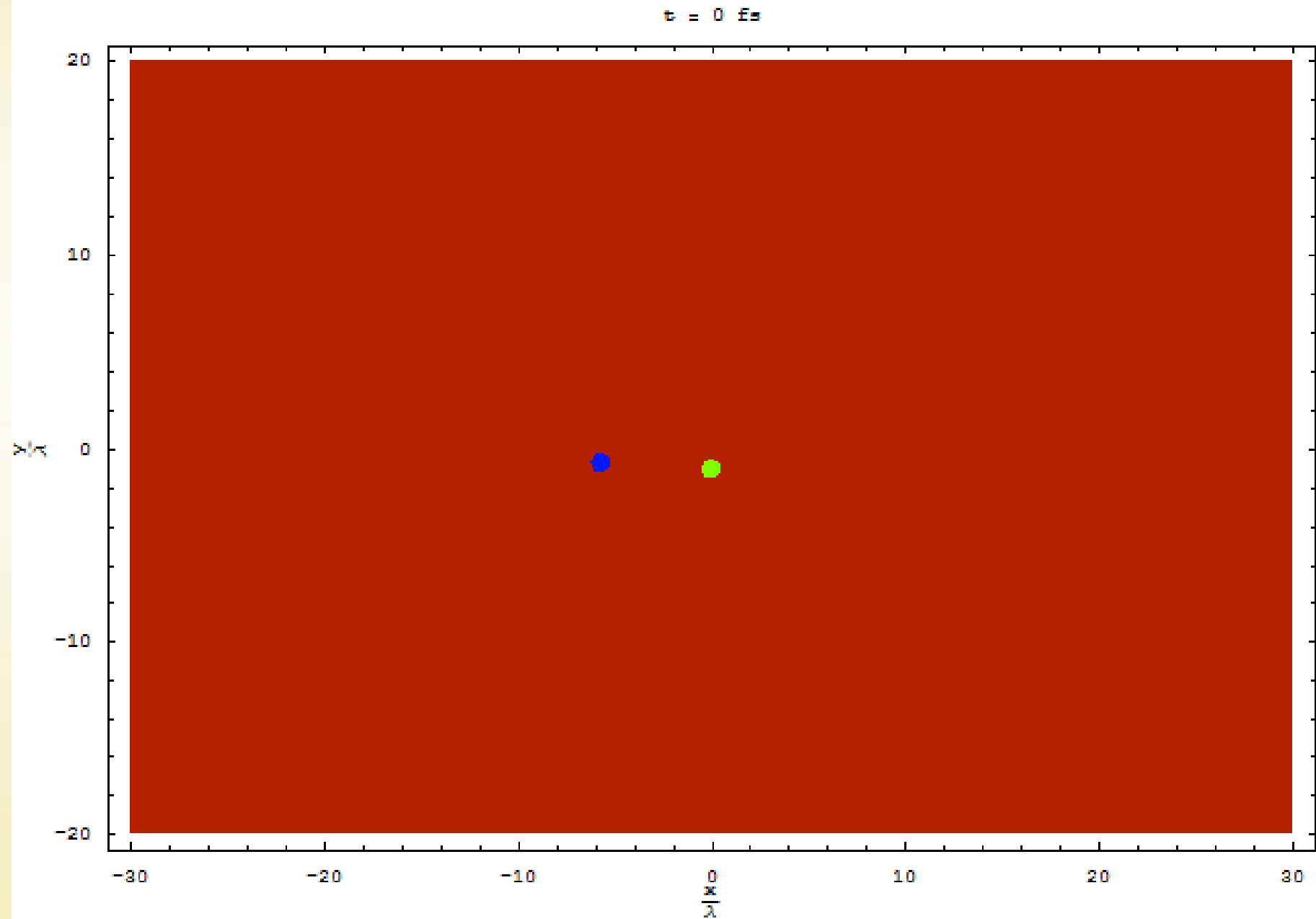
\*K.I.Popov et al, Phys.Plasmas 15, 013108 (2008)

# Plane Wave Launch

$t = 0 \text{ fs}$

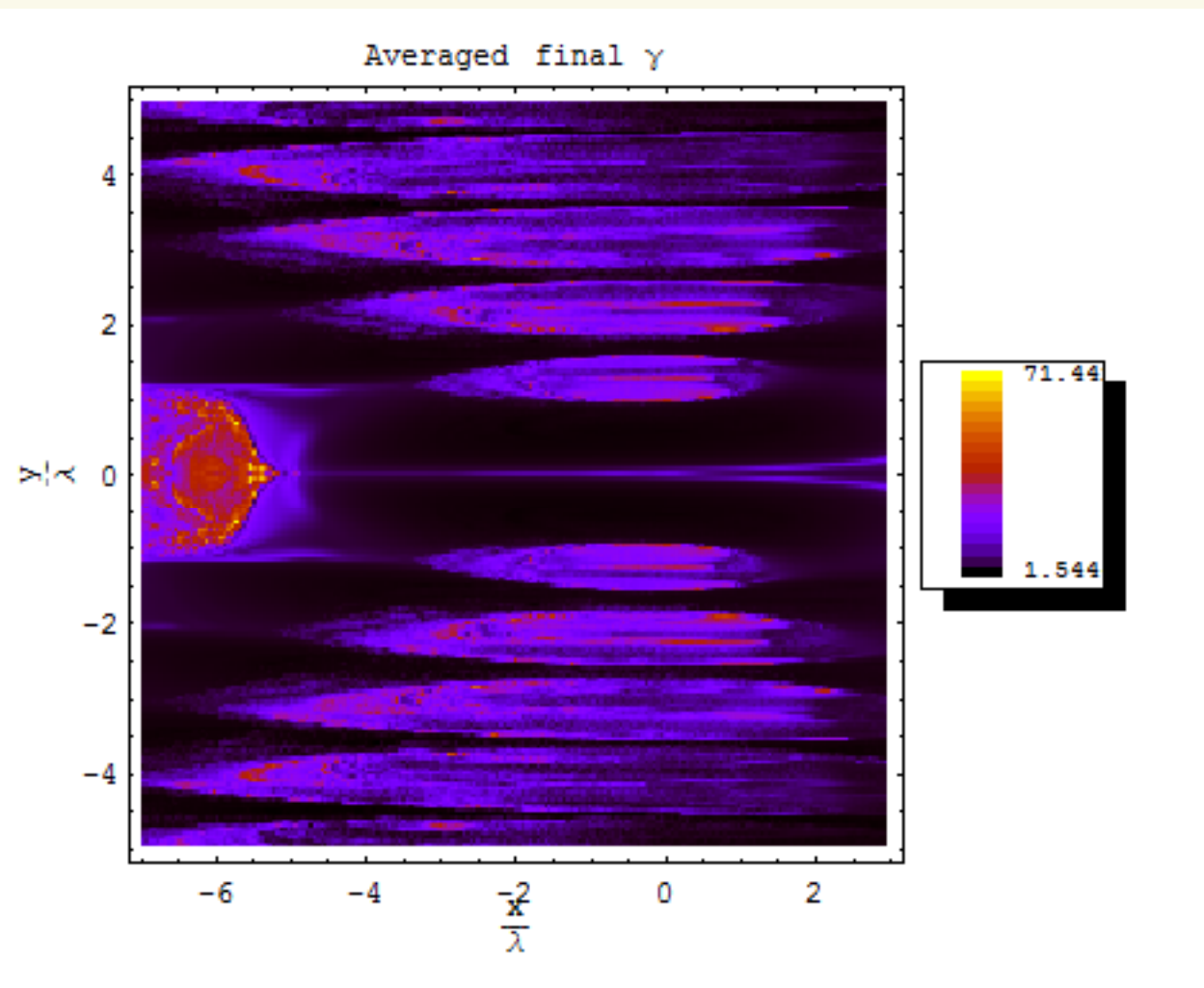


# Tight Focus Case



# Energy map

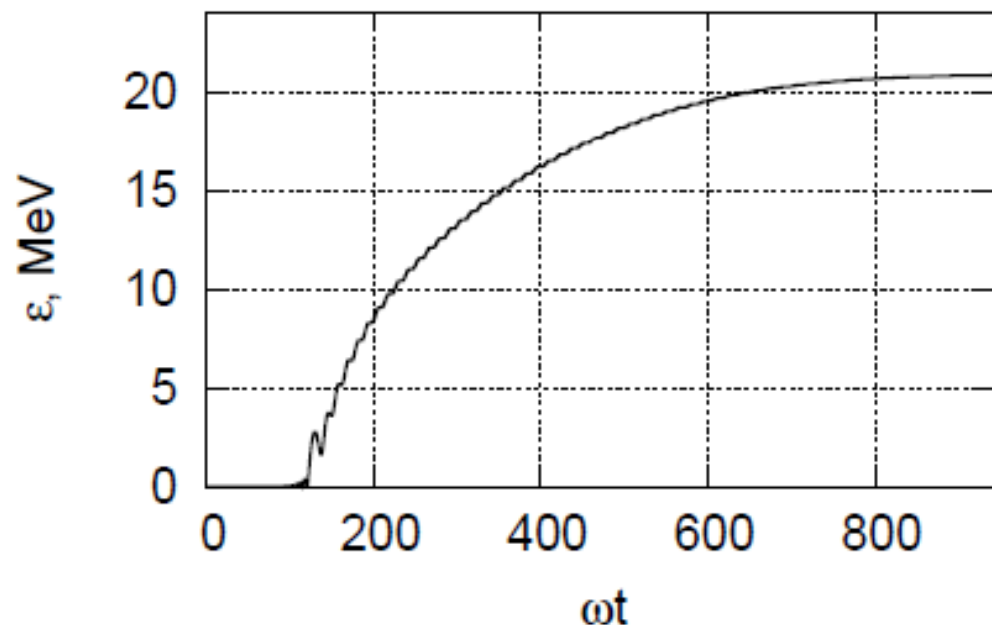
- The final energy depends on the particle initial position and phase.
- Final  $\gamma$ -factor averaged over the laser phase vs. initial position of the particle is the energy map



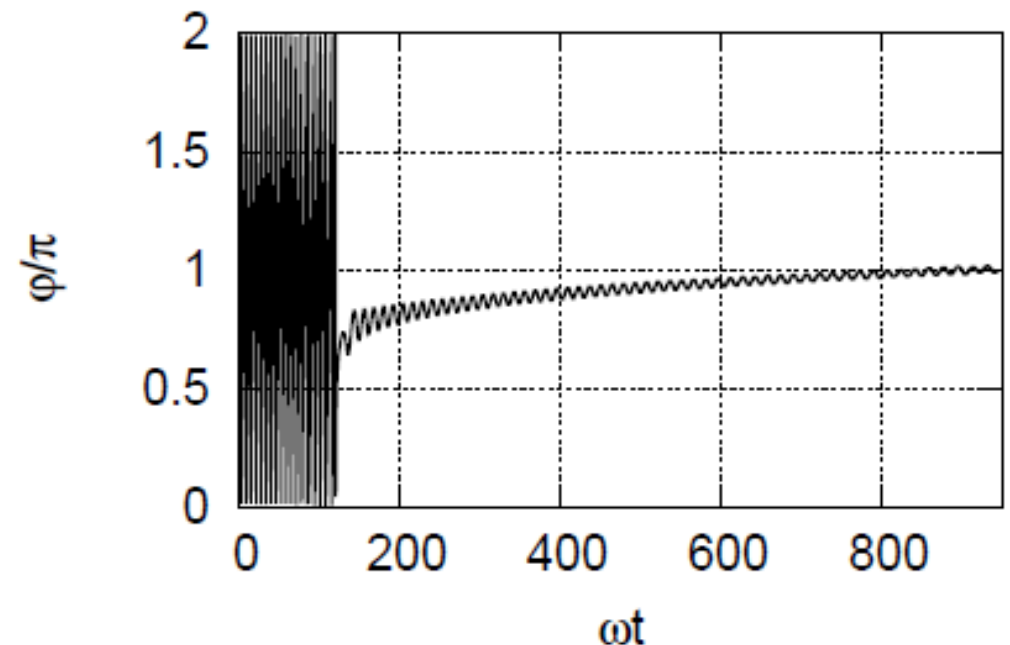
# Acceleration mechanism

Typical acceleration scenario: particle pre-accelerates in a complicated process and then acquires a velocity close to the speed of light. When the velocity is close enough to the speed of light, the particle starts to co-propagate with the pulse. The main energy gain is acquired during the co-propagation with the pulse.

Particle energy:



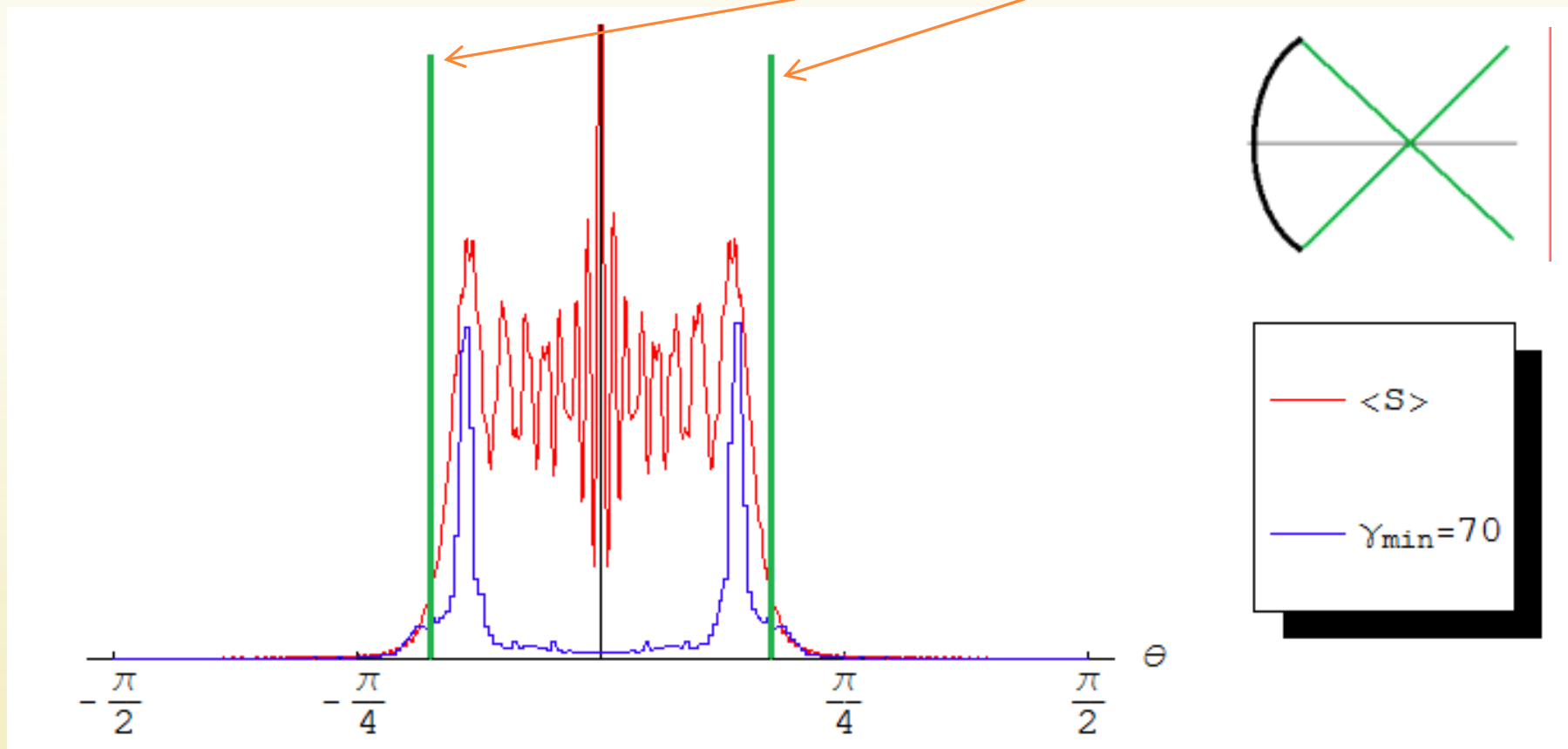
Local field phase:



# Jets formation

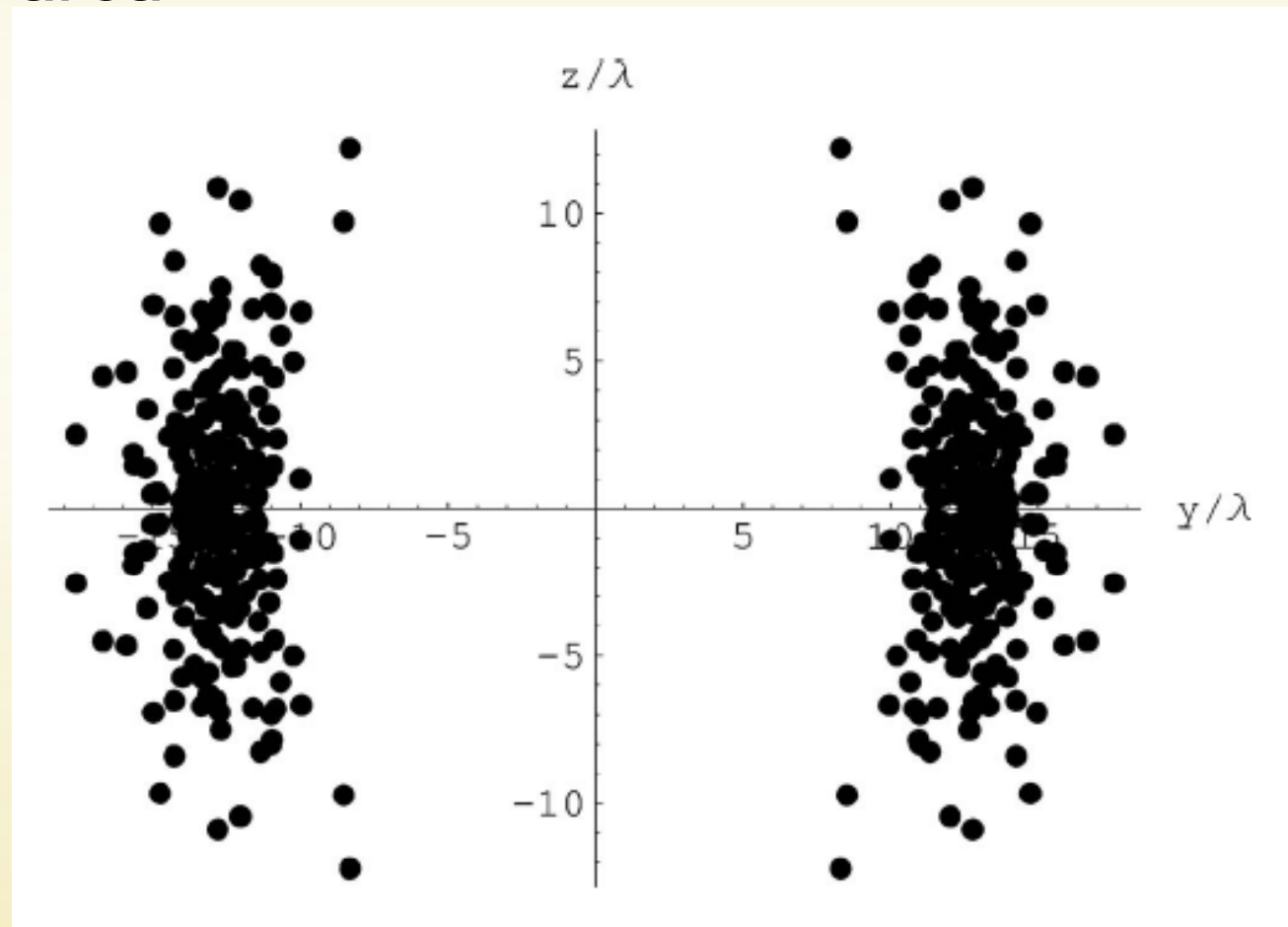
Vacuum acceleration process is characterized by formation of the jets along the laser focusing cone

Geometrical laser cone



# Jets formation

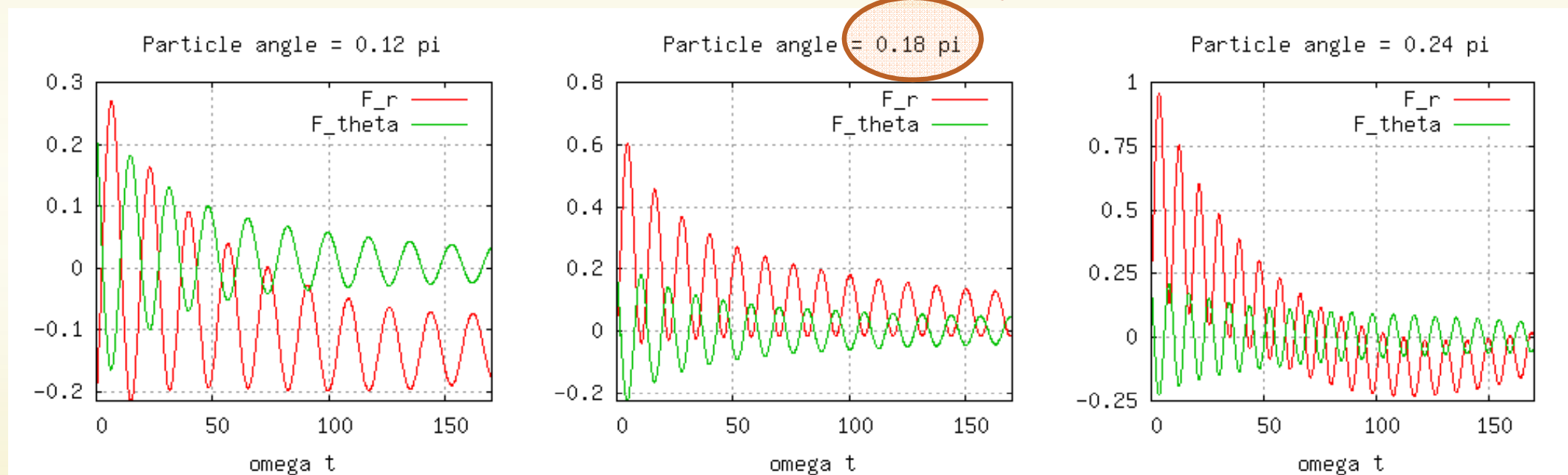
2% of the most energetic particles from the test particle simulations as they would be detected on a screen behind the interaction area



The particles were initially uniformly distributed in the plane perpendicular to the laser propagation

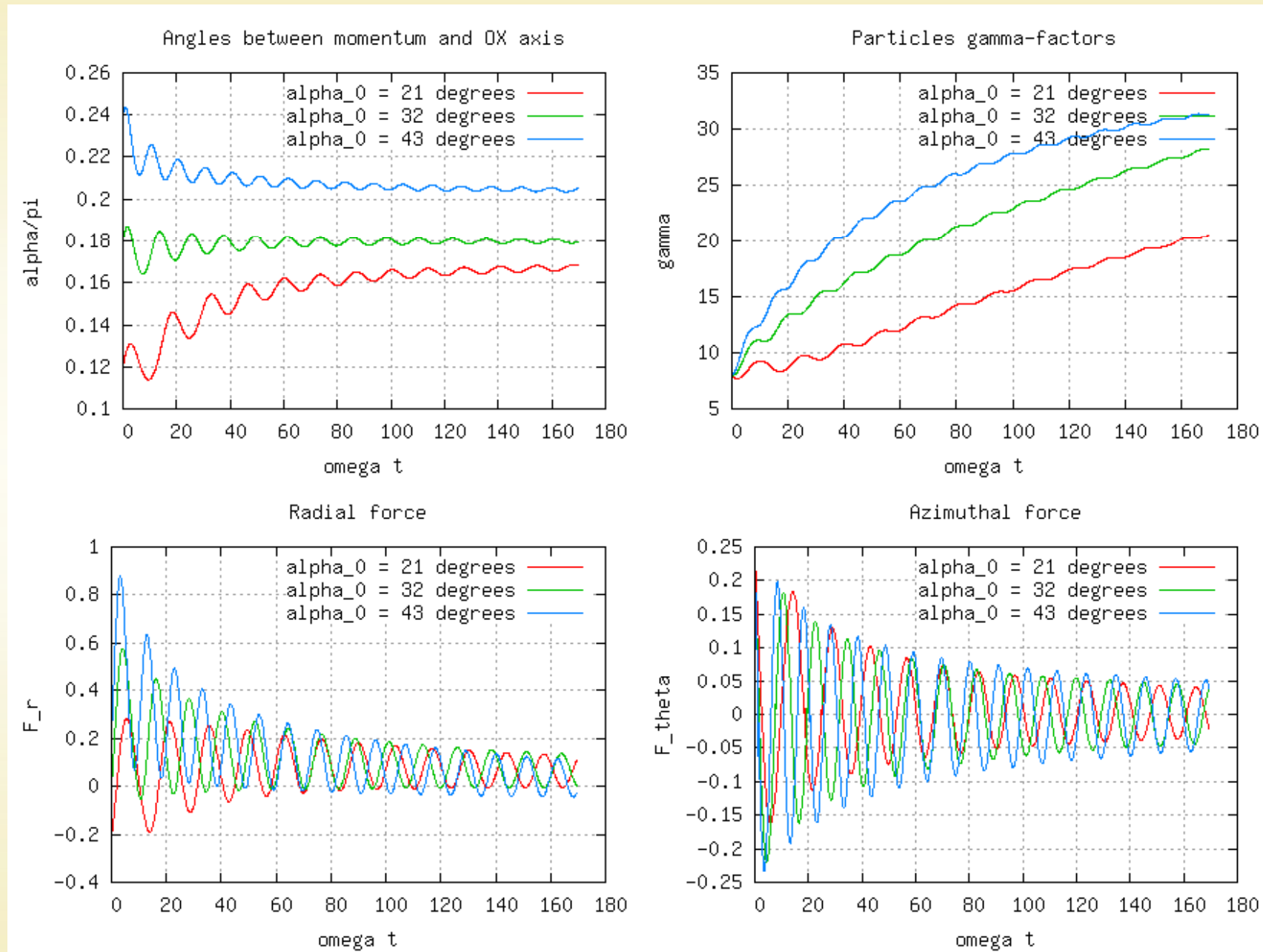
# Jets formation

Preferred angle



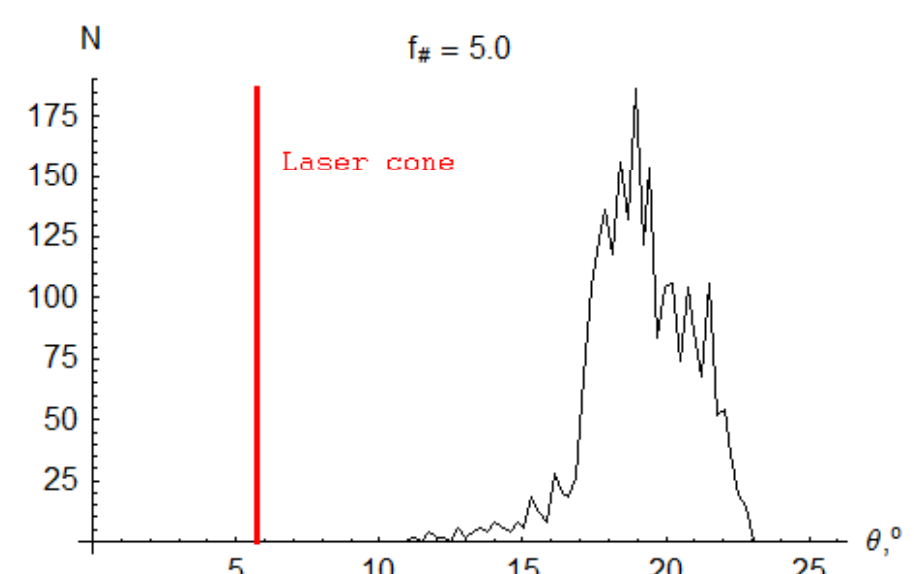
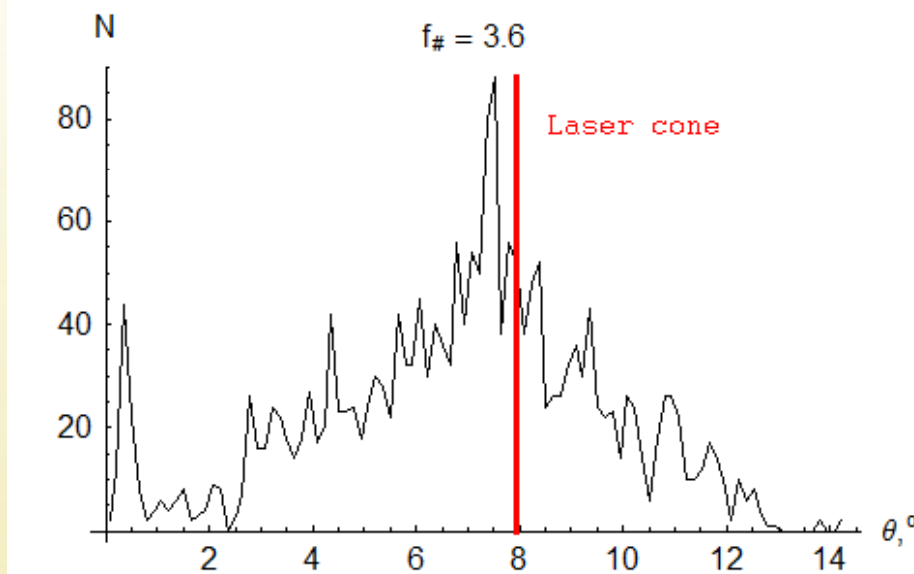
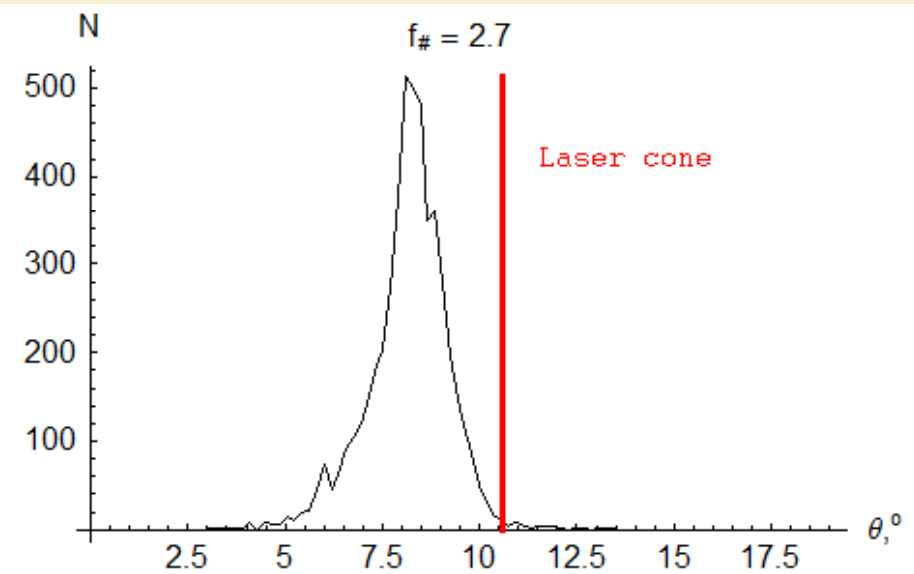
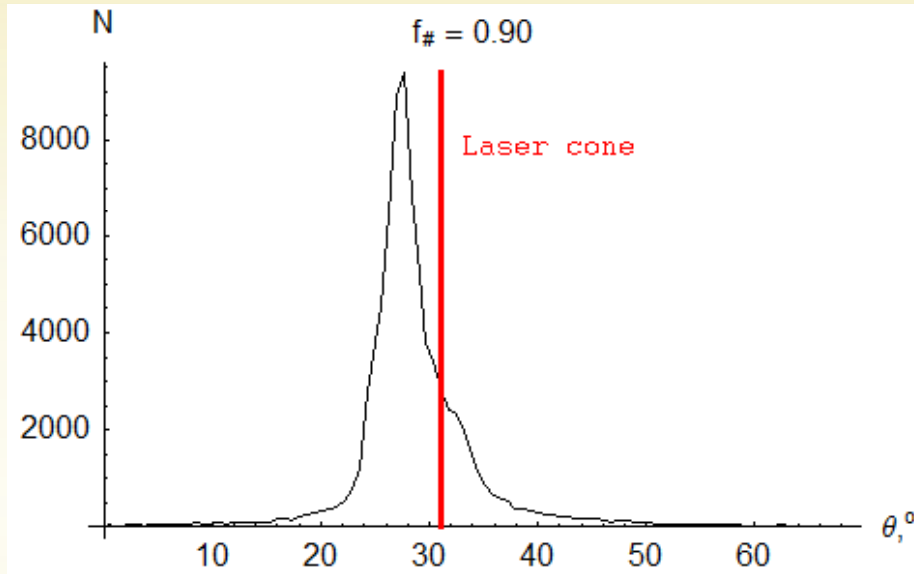
Forces acting onto a hypothetical particle moving with the specified angle to the OX axis with velocity  $0.997c$  ( $\gamma = 12$ )

# Jets formation



Particles injected into a certain point under different angles tend to bend towards the preferred direction

# Jets formation and tightness of focusing



Angular distribution of 5% most energetic particles

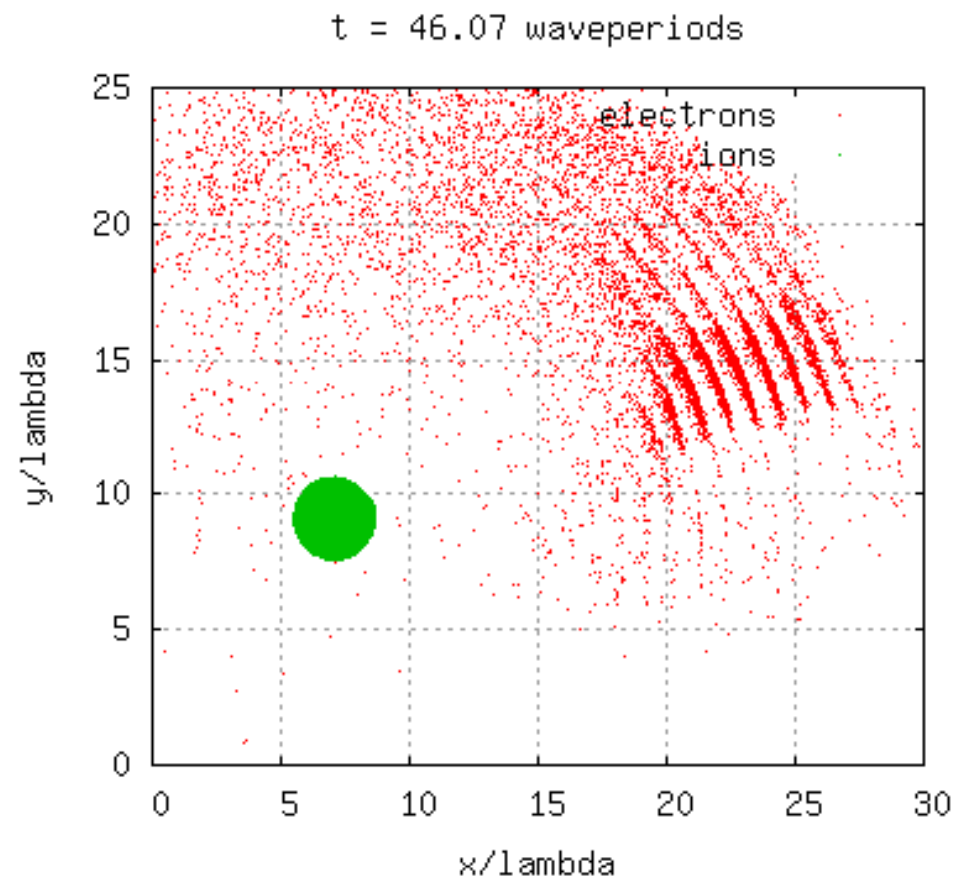
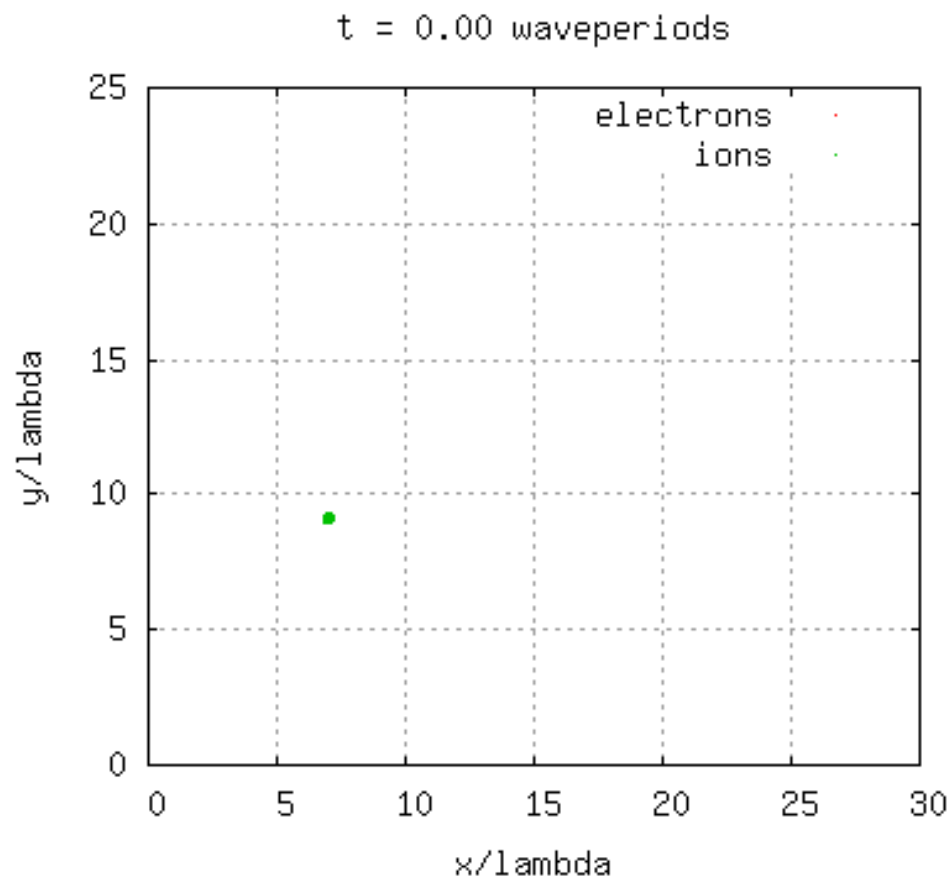
# PIC simulations

- The 3D Particle-In-Cell (PIC) code was used to simulate the interaction between the tightly focused pulse and a plasma configuration
- The fields calculated by Stratton-Chu integrals were used as boundary conditions for the finite-difference Maxwell solver of the PIC code
- Plasma is supposed to be pre-ionized

# Interaction with a cluster

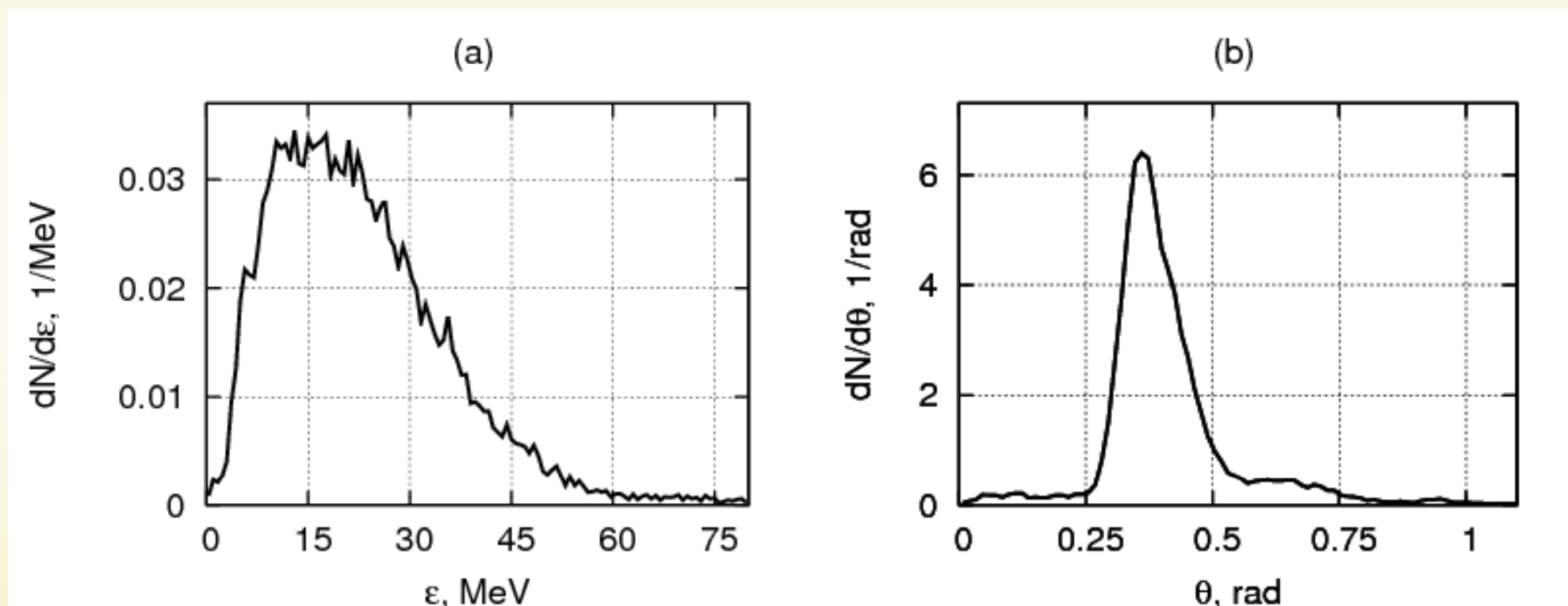
Cluster is a target close to the test particle.

Projections of the particles coordinates onto XY plane from the interaction of a 400 nm cluster of  $n = 25 n_{cr}$  with a 30 fs laser pulse focused by an f-0.9 parabolic mirror. Maximum laser intensity is  $10^{22}$  W/cm<sup>2</sup>. The projection of the laser focus on the pictures is in the point  $(7\lambda; 7\lambda)$ . Simulations are 3D.



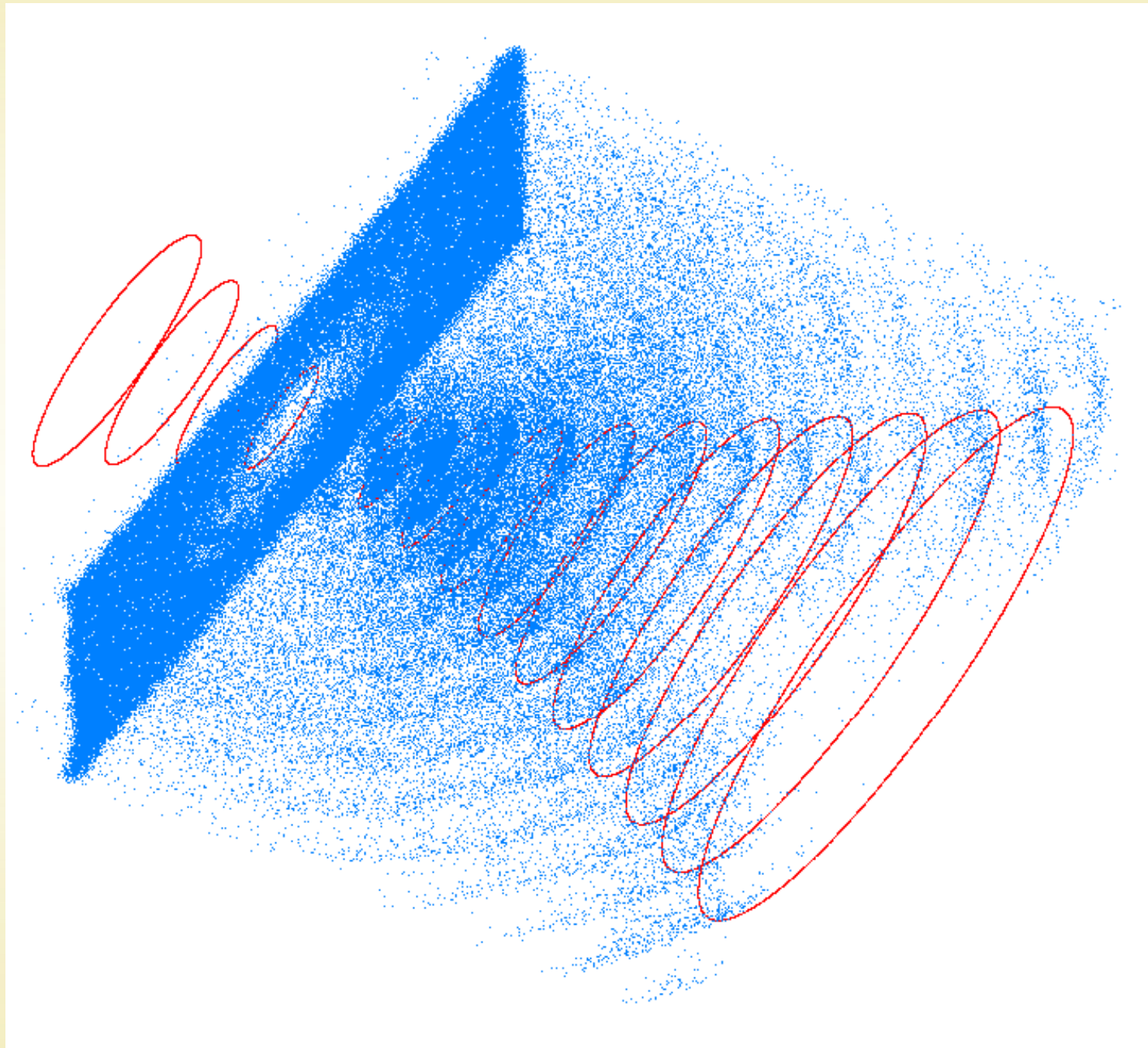
# Interaction with a cluster

Energy spectrum and angular distribution of electrons from interaction between the tightly focused laser and a 400-nm spherical plasma



Estimated number of particles in the jet: up to  $10^8$

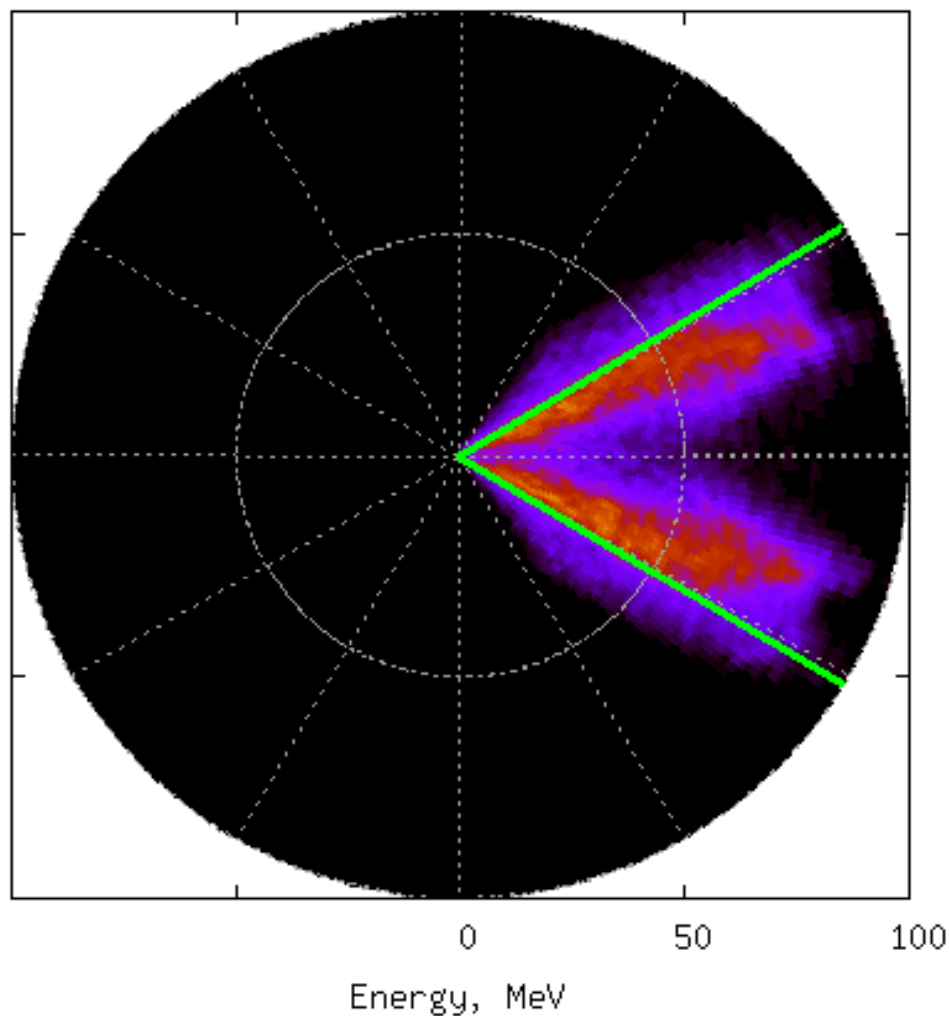
# Interaction with an ultrathin foil



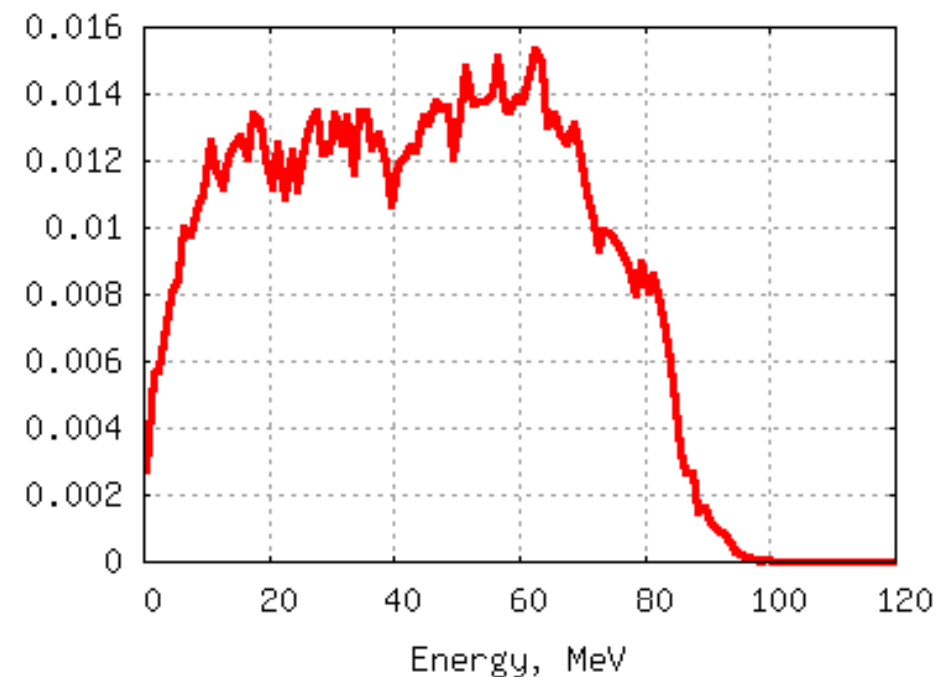
Typical foil parameters:  $n = 50 n_{cr}$ , foil thickness  $\delta \sim 80 - 120$  nm

# Characteristics of the jets

Energy-angle diagram (green lines represent geometrical laser cone):

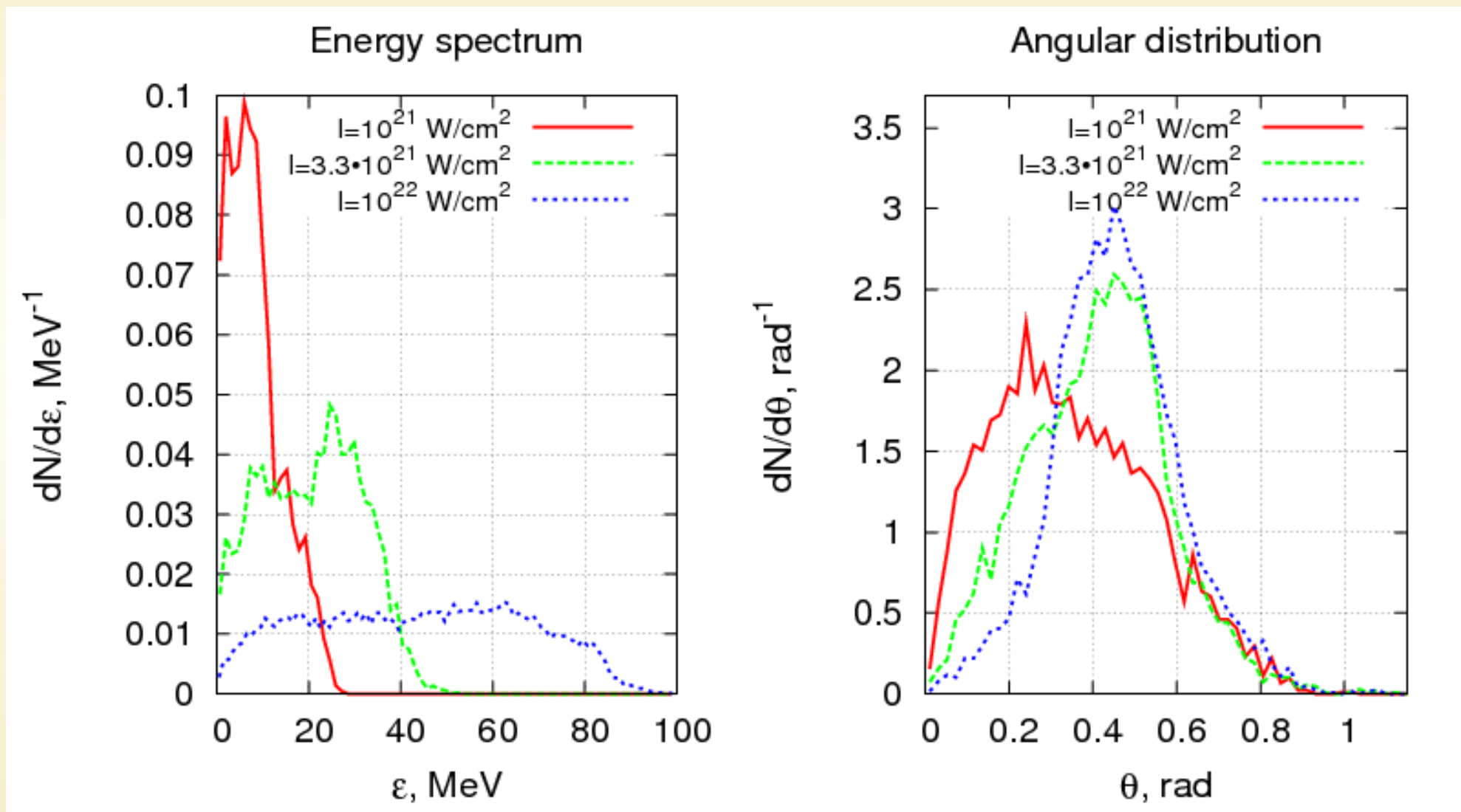


Spectrum of the particles within  $10^\circ$  of the maximum jet density:



Estimated number of electrons within  $10^\circ$  of the maximum jet density:  $10^8$  for  $\sim 10^{10}$  in the focal spot

# Dependence of particles spectrum and angular distribution on laser intensity



Foil density  $50 n_{cr}$ , foil thickness 80 nm

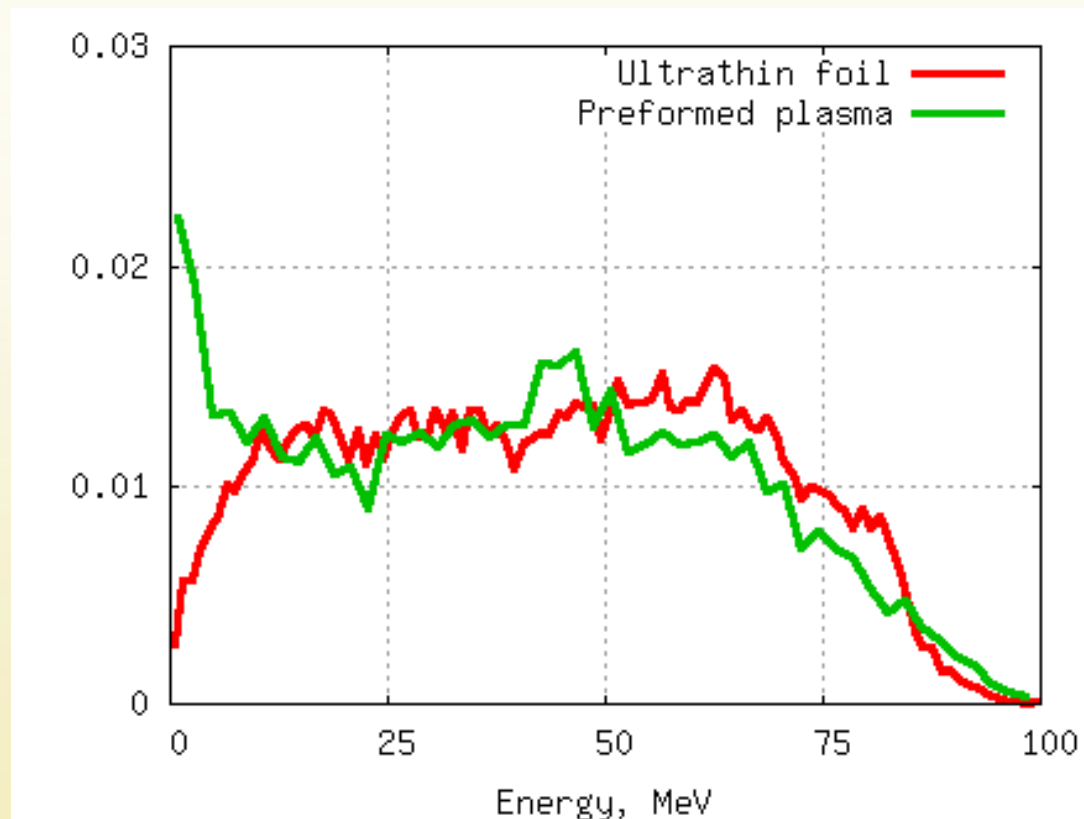
# Conclusions

- Test particle and PIC simulations of electron acceleration in the field of a tightly focused laser being numerical solution to the Maxwell equation are performed
- Quasi-monoenergetic spectra of electrons are observed for interaction of the pulse with special nanotargets
- Spreading out of plasma slightly worsen the resulting spectra
- Up to  $10^8$  electrons having energies between 10 and 80 MeV and moving within angle of  $10^\circ$  is possible with an f-0.9 mirror focused laser of maximal intensity  $10^{22}$  W/cm<sup>2</sup> with a high contrast ratio

# Preformed plasma

- The same charge, but spread out
- May be a consequence of the laser prepulse

$$n(x) = n_0 \exp\left[-\frac{(x-x_0)^2}{\Delta x^2}\right], \quad \Delta x \sim \text{few microns}, \quad 1 \mu\text{m below}$$



$$n_0 = 2.8 n_{cr}$$

The charge is equal to that of an ultrathin foil of  $n = 50 n_{cr}$  and thickness of 80 nm.